

## Lecture 6: Risk/Return in Financial Markets

ECON435: Financial Markets and the Macroeconomy

Anton Korinek

Spring 2011

1

## Interest Rates

Interest Rate = promised rate of return

$R$  ... nominal interest rate: in dollar terms

$r$  ... real interest rate: in terms of purchasing power  
= adjusted for inflation rate  $i$

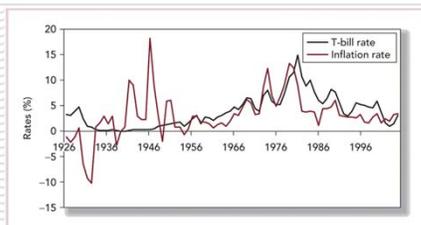
relationship:  $r \approx R - i$  (Fisher equation)

[ more precisely:  $1+r = (1+R)/(1+i)$  ]

measurement of inflation:  
increase in consumer price index (CPI)

2

## Interest and Inflation Rates



3

## Risk-free Interest Rates

"Risk-free" interest rates: no default risk

### Caveats:

- no investment is truly risk-free
- guaranteed nominal return does not protect against fluctuations in purchasing power

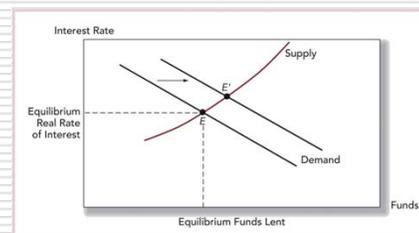
4

## Determinants of Real Interest Rates

- Demand
- Supply
- Fed Policy
- Inflation Expectations

5

## Determinants of Real Interest Rates



6

## Comparing Rates of Return

Effective Annual Rate (EAR):

- incorporates compounding effect
- $FV = (1 + EAR)^n PV$

Annual Percentage Rate (APR):

- for subannual periods
- ignores compounding effect:  
 $APR = nr_n$  where  $r_n$  is return in each of  $n$  subperiods
- e.g. credit card that charge 3% monthly:  
 $APR = 12 * 3\% = 36\%$   
 $EAR = (1 + 3\%)^{12} - 1 = 42.6\%$

7

## Comparing Rates of Return

For risky investments:

$$\text{Holding-period return (HPR)} = \frac{\text{Price increase} + \text{dividends}}{\text{Initial price}}$$

Expected return =  $E[\text{HPR}]$

Standard deviation =  $\sigma$

Risk premium =  $E[\text{HPR}] - \text{Risk-free rate}$

8

## Sharpe Ratio

Sharpe ratio =

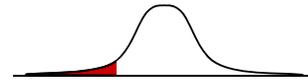
$$= \frac{\text{Risk premium}}{\text{Std. dev.}}$$

- first proposed by William Sharpe
- measures the "risk-weighted" excess return

9

## Value at Risk (VaR)

- Value-at-Risk = quantile of the return distribution  
= measure of loss under extreme market conditions
- typically 5% quantile (or 5<sup>th</sup> percentile) is used



- **Interpretation:** the loss on an investment will be larger than the 5% VaR with 5% probability  
→ important in risk management systems to limit the maximum loss
- **Example:** VaR at Goldman Sachs for daily trading losses was \$250m in 2010 (up from \$125m in 2007)

10